

Chapter 3

Formulas, Equations, and Moles: II



Amounts of Reactants and Products

- In lab, we want to predict amount of product we can expect from a reaction
- Have to use **stoichiometry**: quantitative study of reactants and products in a reaction (mole to mole ratio)
- Use the **mole** to relate one substance in a reaction to another (equation coefficients, see Table 3.1)
 - ♦ $2\text{H}_2(\text{g}) + \text{O}_2(\text{g}) \rightarrow 2\text{H}_2\text{O}(\text{g})$

Mole Ratios



- We use coefficients in a balanced equation to determine the mole ratio in which substances need to react.
- $\text{MgCl}_2(\text{aq}) + 2\text{AgNO}_3(\text{aq}) \rightarrow 2\text{AgCl}(\text{s}) + \text{Mg}(\text{NO}_3)_2(\text{aq})$
 - ♦ 1 molecule of MgCl_2 reacts with 2 molecules of AgNO_3 to produce 2 molecules of AgCl and 1 molecule of $\text{Mg}(\text{NO}_3)_2$
 - ♦ Molecules are not practical! Scale up to moles!

Stoichiometry Calculations

- Mole to mole conversions
- $\text{MgCl}_2(\text{aq}) + 2\text{AgNO}_3(\text{aq}) \rightarrow 2\text{AgCl}(\text{s}) + \text{Mg}(\text{NO}_3)_2(\text{aq})$
1.00 mol excess ?
- How many moles of solid product do you predict to form?

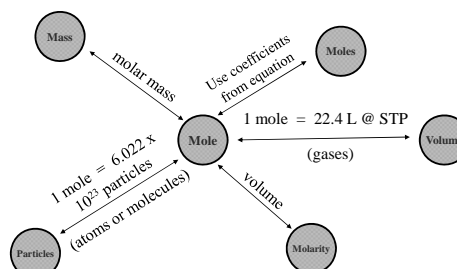


- Cannot compare grams of one to grams of another!!

Mole Ratios

- Calculate moles of ppt that can be made in the following reactions. Predict products and phases first.
- $\text{NaCl}(\text{aq}) + \text{Hg}(\text{NO}_3)_2(\text{aq}) \rightarrow$
 - ♦ 0.500 mol NaCl
- $\text{FeCl}_3(\text{aq}) + \text{NaOH}(\text{aq}) \rightarrow$
 - ♦ 2.35 mol NaOH
- $\text{Li}_2\text{SO}_4(\text{aq}) + \text{AgCH}_3\text{COO}(\text{aq}) \rightarrow$
 - ♦ 0.1098 mol AgCH_3COO

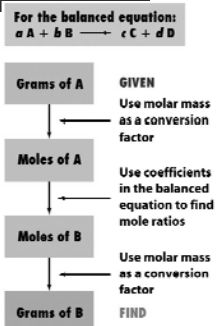
Mole Diagram



Courtesy: www.unit5.org/christjs/Stoichiometry/Mole%20Island%20Diagram.ppt

Amounts of Reactants and Products

- We can balance a chemical equation to find relative amounts of reactants and products.
- How can we predict the amount of product we should get?
- Worked Ex. 3.5 – 3.7; Problems 3.7, 3.8



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Stoichiometry Calculations

- Mass to mass conversions
- Given mass of reactant, find mass of precipitate:
- $MgCl_2 + 2 AgNO_3 \rightarrow 2 AgCl + Mg(NO_3)_2$
- 1.2482 g $MgCl_2$ and excess $AgNO_3$
 - ♦ Find number of moles of $MgCl_2$ using molar mass
 - ♦ Find number of moles of $AgCl$ using mol:mol ratio
 - ♦ Find number of grams of $AgCl$ using molar mass

Mass to Mass Conversions

- How many grams of $KClO_3$ are needed to completely destroy one gummy bear? (Gummy bears have an average mass of 2.4882 g. Roughly 50% of a gummy bear's mass is sucrose - $C_{12}H_{22}O_{11}$.)
- $_KClO_3(l) + _C_{12}H_{22}O_{11}(s) \rightarrow _KCl(l) + _CO_2(g) + _H_2O(g)$

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Group Work

- $Al(NO_3)_3 + NaOH \rightarrow Al(OH)_3 + NaNO_3$
- 10.54 g xs ?
- How many grams of aluminum hydroxide can be made by starting with 10.54 grams of aluminum nitrate? (Hint: Is the equation balanced?)

Yields of Chemical Reactions

- If you ran that reaction in lab and only obtained 3.18 g (actual yield) of $Al(OH)_3$, what percent of the maximum did you obtain?
- Percent yield = Actual / Theoretical x 100%
- Theoretical will be calculated; actual yield will be given in a problem (or obtained in lab)
- Worked Ex. 3.8, 3.9; Problems 3.9, 3.10

Limiting Reactants

- Analogy: making martinis
- I have 7 martini glasses, 36 olives, 12 shots of vodka, and 8 stirrers
- Each martini requires 1 glass, 2 olives, 2 shots of vodka, and 1 stirrer
- How many martinis can I make?



Limiting Reactant

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Limiting Reagents: $2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$

Before reaction

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Limiting Reagents

$2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$

What is the limiting reactant?

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Limiting Reagents

$2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$

What is the limiting reactant?

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Limiting Reagents

$2\text{H}_2 + \text{O}_2 \rightarrow 2\text{H}_2\text{O}$

What is the limiting reactant?

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Group Work

- $\text{Al}(\text{NO}_3)_3 + 3\text{NaOH} \rightarrow \text{Al}(\text{OH})_3 + 3\text{NaNO}_3$
- 10.54 g 10.54 g ?
- How many grams of aluminum hydroxide can be made by starting with 10.54 grams of aluminum nitrate and 10.54 grams of sodium hydroxide?

Limiting Reagent Calculations

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    Mass of limiting reactant
      ↓
    moles of limiting reactant
      ↓
    moles of product
      ↓
    mass of product (theoretical yield)
  
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Limiting Reagent Calculations

- How do we determine, mathematically, which is the limiting reagent?
- Two ways:
 - Compare moles of each reactant required to consume all of other reactant (example on next slide).
 - Calculate moles of desired product from each reactant.

Whichever REACTANT produces less product (and gets used up first) is the limiting reactant (or reagent).

Limiting Reagent Calculations

- $\text{Al}(s) + \text{Cl}_2(g) \rightarrow \text{AlCl}_3(s)$
- 1.67 g Al (0.06189 mol) and 1.67 g (0.02355 mol) Cl_2
- Moles of Al needed to use up all Cl_2 :
 - ♦ $0.02355 \text{ mol Cl}_2 \times (2 \text{ mol Al} / 3 \text{ mol Cl}_2) = 0.0157 \text{ mol Al}$
 - ♦ Started with 0.06189 mol Al, but we only need 0.0157 to use up Cl_2 ; Cl_2 is limiting reagent
- Moles of Cl_2 needed to consume Al:
 - ♦ $0.06189 \text{ mol Al} \times (3 \text{ mol Cl}_2 / 2 \text{ mol Al}) = 0.09284 \text{ mol Cl}_2$
 - ♦ We need 0.09284 mol Cl_2 to use up all of the Al but we only started with 0.02355 mol; Cl_2 is limiting reagent.

Group Work

- $2\text{Al}(s) + 3\text{Cl}_2(g) \rightarrow 2\text{AlCl}_3(s)$
- Method 2: use each reactant to calculate mass of product that can be formed.
- 1) If we begin with 1.67 g Al (s) and 1.67 g Cl_2 (g), which is the limiting reactant?
- 2) How many grams of $\text{AlCl}_3(s)$ will, theoretically, be produced?
- 3) What is the percent yield if you obtained 1.76 g AlCl_3 in the lab?
- 4) How many grams of the excess reagent will be left over?

Group Work

- 3.71 Hydrogen and chlorine react to yield hydrogen chloride. How many grams of HCl are formed from reaction of 3.56 g of hydrogen and 8.94 grams of chlorine?
- Worked Ex. 3.10, Problem 3.11, 3.12

Solution Stoichiometry Example

- Consider the reaction:
 - ♦ $3\text{CaCl}_2(aq) + 2\text{Na}_3\text{PO}_4(aq) \rightarrow \text{Ca}_3(\text{PO}_4)_2(s) + 6\text{NaCl}(aq)$
- If we mix 25.0 mL of 0.200 M CaCl_2 solution with 50.0 mL of 0.250 M Na_3PO_4 solution, what mass of precipitate is formed?

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Concentration of Solutions: Molarity

- **Concentration:** amount of solute present in a given amount of solution
- **Molarity:** moles of solute in 1 L of solution
 - ♦ moles solute / liters solution; $M = \text{mol} / L$
- Allows us to calculate 1) mass of solid needed to make a solution of a certain concentration or 2) concentration of solution if mass and volume are known.
- 1.00 M NaCl = 1.00 mol NaCl in 1 L solution

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Concentration of Solutions: Molarity

- 1.00 M NaCl = 1.00 mol NaCl in 1 L solution
- 0.500 M NaCl = 0.500 mol NaCl in 1 L sol'n.
- To find moles of solute, $M \cdot V = \text{mol}$
- **How many moles in 5.67 mL of 0.500 M NaCl?**
- Worked Ex. 3.11, 3.12, Problems 3.14 – 3.17

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Concentration of ions

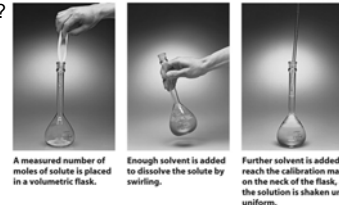
- What is the concentration of Cl^- ions in a 0.150 M FeCl_3 solution?
- $1 \text{ mol FeCl}_3 \rightarrow 1 \text{ mol Fe}^{3+} + 3 \text{ mol Cl}^-$
- $0.150 \text{ M FeCl}_3 \times (3 \text{ mol Cl}^- / 1 \text{ mol FeCl}_3) = 0.450 \text{ M Cl}^-$

Concentration of Solutions

- We can calculate concentration (molarity) if we know mass and volume.
 - ♦ $\text{Mass solute} \div \text{molar mass} = \text{moles solute}$
 - ♦ $\text{Moles solute} \div \text{volume solution} = \text{Molarity}$
- Or we can calculate the mass of solute needed to make a solution of certain concentration (molarity).
 - ♦ $\text{Molarity} \cdot \text{volume solution} = \text{moles solute}$
 - ♦ $\text{Moles solute} \cdot \text{molar mass} = \text{mass solute needed}$

Concentration Calculations

- What is the concentration of a 1.00 L solution made by dissolving 5.00 g NaCl in water?
- 5.00 grams NaCl in a 500.0 mL solution?
- What mass of NaCl do we need to make 1.00 L of a 0.500 M solution?



Concentration of Solutions – Mad Libs

- 1) Water-soluble ionic compound
- 2) Number greater than 500
- 3) Number between 0 and 1
- 4) Number between 1 and 5
- 5) Any water-soluble compound
- 6) Number between 500 and 1000

Concentration of Solutions - Mad Libs

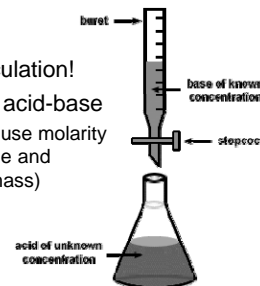
- How many grams of (1) _____ are required to prepare a (2) _____ mL solution whose concentration is (3) _____?
- What is the concentration of a solution made by adding (4) _____ grams of (5) _____ to _____ mL of water?

Titration

- **Titration:** method of determining the concentration (or volume) of an unknown solution by using a solution with a known concentration (standard)
 - ◆ moles = $M \cdot V$
- Equivalence point: point at which acid has completely reacted with and been neutralized by base (moles acid = moles base)
- End point: point at which the indicator changes color (slight change in solution's pH)

Titration set-up

- Titrant in buret
- Unknown in flask
- Can't use dilution calculation!
- Need mol-mol ratio of acid-base
- **Solution stoichiometry:** use molarity to convert between volume and moles (instead of molar mass)
 - ◆ $M = \text{mol} / L$
 - ◆ $\text{mol} = M \cdot L$
 - ◆ $L = \text{mol} / M$



Titration

- 23.78 mL of 0.2500 M NaOH neutralized 20.00 mL of HCl. What is the concentration of HCl? Start with a balanced equation.

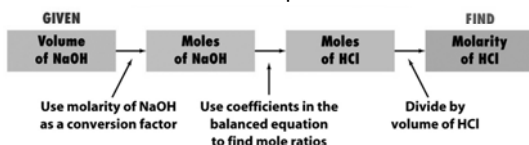


Figure 3-4 Chemistry, 5/e
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- Worked Ex. 3.14, Problems 3.20, 3.21, 3.22

Dilution

- **Dilution:** lowering the concentration of solution (by adding water)
 - ◆ number of moles of solute stays the same, amount of solvent increases
- The number of moles of **solute** stays the same; volume increases (lower molarity)
 - ◆ moles = $M \cdot V$
 - ◆ $M_{\text{conc}} \cdot V_{\text{conc}} = M_{\text{dil}} \cdot V_{\text{dil}}$ or $M_1 V_1 = M_2 V_2$
- Example: What is the **final** concentration of solution made by adding 100.0 mL of 3.00 M HCl to 300.0 mL of DI water?

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Dilution

- How would you prepare 500.0 mL of 0.500 M H_2SO_4 starting with concentrated (18.0 M) solution? (Hint: What variable are you solving for?)
 - ◆ Remember to add acid to water.
- How much **water** do you need to add to 25.0 mL of a 4.50 M NaOH solution to make a 1.00 M NaOH solution?
- Worked Ex. 3.13; Problems 3.18, 3.19
- 1) 87.5 mL of water added to 25.0 mL of 4.50 M NaOH; 2) 13.9 mL of 18.0 M H_2SO_4

Group Work

- How many mL of 1.018 M H_2SO_4 are needed to neutralize 20.00 mL of 0.9989 M NaOH?
 - ◆ Write balanced equation
 - ◆ Determine number of moles of known
 - ◆ Calculate mole ratio to determine moles of unknown
 - ◆ Divide by concentration to find volume

Percent Composition of Compounds

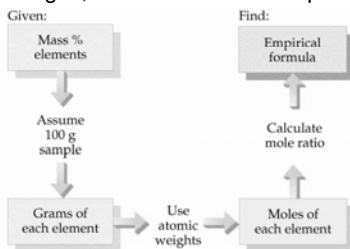
- Percent by mass: percent by mass of each element in a compound
- H_2O_2
 - ◆ 2 moles H, 2 moles O
 - ◆ $\text{H} = 2 \text{ mol} \times 1.008 \text{ g/mol H} = 2.016 \text{ g H}$
 - ◆ $\text{O} = 2 \text{ mol} \times 16.00 \text{ g/mol O} = 32.00 \text{ g O}$
 - ◆ $\text{H}_2\text{O}_2 = 2.016 \text{ g H} + 32.00 \text{ g O} = 34.02 \text{ g}$
 - ◆ $\% \text{H} = 2.016 \text{ g H} / 34.02 \text{ g H}_2\text{O}_2 \times 100\% = 5.926\%$
- What is %O? Solve 2 ways.....

Percent Composition of Compounds

- What is the percent by mass of Cr, S, and O in $\text{Cr}_2(\text{SO}_4)_3$?

Percent Composition of Compounds

- We can reverse this calculation.
- Know percentages, need to calculate empirical formulas.



Empirical Formulas

- Calculate the empirical formulas:
 - ◆ 50% S, 50% O
 - ◆ 43.64% P, 56.36% O
- Assume 100 g of the material:
 - ◆ $50 \text{ g O} \times 1 \text{ mol} / 16.0 \text{ g} = 3.125 \text{ mol O}$
 - ◆ $50 \text{ g S} \times 1 \text{ mol} / 32.066 \text{ g} = 1.559 \text{ mol S}$
 - ◆ $\text{mol O} / \text{mol S} = 3.125 / 1.559 = 2.004$ or 2
 - ◆ SO_2
- Assume 100 g of material:
 - ◆ $43.64 \text{ g P} \rightarrow \text{mol P} (1.4089 \text{ mol P})$
 - ◆ $56.36 \text{ g O} \rightarrow \text{mol O} (3.5225 \text{ mol O})$
 - ◆ Ratio of two moles (2.5 O / 1 P); need whole numbers

Molecular Formulas

- We just found the empirical formula to be P_2O_5 . This compound has a molecular mass of 141.9 g/mol.
- We know the molecular formula has a molar mass of 283.8 g/mol. How many multiples of P_2O_5 do we need to reach a mass of 283.8?
- Worked Ex. 3.15 – 3.17; Problems 3.24 – 3.29

Practice Problem

- A compound contains 30.4 % nitrogen and 69.6 % oxygen. The molecular mass of the compound is 92 g/mol.
 - ◆ What is the empirical formula of the compound?
 - ◆ What is the molecular formula of the compound?

Group Work

- A compound contains 40.00% C, 6.71% H, and the rest is O. Determine the empirical formula of this compound.
- If the molar mass of the substance is 180.16 g/mol, determine the molecular formula of this substance.